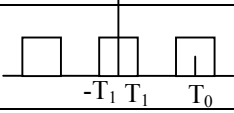


**Tabelul 4.2. Proprietățile transformării Fourier în timp**

Semnalul aperiodic	Transformata Fourier
$x(t)$	$X(\omega)$
$y(t)$	$Y(\omega)$
$a x(t) + b y(t)$	$a X(\omega) + b Y(\omega)$
$x(t - t_0), t_0 \in R$	$e^{-j\omega t_0} X(\omega)$
$e^{j\omega_0 t} x(t), \omega_0 \in R$	$X(\omega - \omega_0)$
$x^*(t)$	$X^*(-\omega)$
$x(-t) = x(t)$	$X(-\omega)$
$x(at), a \in R$	$\frac{1}{ a } X\left(\frac{\omega}{a}\right)$
$x(t) * y(t)$	$X(\omega) \cdot Y(\omega)$
$x^*(\tau) * y(\tau)$	$X^*(\omega) \cdot Y(\omega)$
$x(t) \cdot y(t)$	$\frac{1}{2\pi} X(\omega) * Y(\omega)$
$\frac{d}{dt} x(t)$	$j\omega X(\omega)$
$\int_{-\infty}^t x(\tau) d\tau$	$\frac{1}{j\omega} X(\omega) + \pi X(0) \delta(\omega)$
$t x(t)$	$j \frac{d}{d\omega} X(\omega)$
$x(t) \in R$	$X(\omega) = X^*(-\omega)$ $ X(\omega)  =  X(-\omega) ; \text{Arg } X(\omega) = -\text{Arg } X(-\omega)$ $\text{Re}\{X(\omega)\} = \text{Re}\{X(-\omega)\}$ $\text{Im}\{X(\omega)\} = -\text{Im}\{X(-\omega)\}$
$x_p(t) \leftrightarrow \text{Re}\{X(\omega)\} \quad x_i(t) \leftrightarrow j \text{Im}\{X(\omega)\}$	
$\int_{-\infty}^{\infty}  x(t) ^2 dt = \frac{1}{2\pi} \int_{-\infty}^{\infty}  X(\omega) ^2 d\omega$	
$x(t) \leftrightarrow X(\omega)$	
$X(t) \leftrightarrow 2\pi x(-\omega)$	

**Tabelul 4.3. Perechi semnal - transformat**

Semnalul	Transformata Fourier	Coefficienții seriei exponențiale (pentru semnale periodice)
$\sum_k c_k e^{jk\omega_o t}$	$\sum_k 2\pi c_k \delta(\omega - k\omega_o)$	$\{c_k\}$
$e^{j\omega_o t}$	$2\pi \delta(\omega - \omega_o)$	$c_1 = 1 ; c_k = 0, k \neq 1$
$\cos \omega_o t$	$\pi [\delta(\omega - \omega_o) + \delta(\omega + \omega_o)]$	$c_1 = c_{-1} = \frac{1}{2} ; c_k = 0, k \notin \{-1, 1\}$
$\sin \omega_o t$	$\frac{\pi}{j} [\delta(\omega - \omega_o) - \delta(\omega + \omega_o)]$	$c_1 = -c_{-1} = \frac{1}{2j} ; c_k = 0, k \notin \{-1, 1\}$
$x(t) = 1(\text{constanta})$	$2\pi \cdot \delta(\omega)$	$c_0 = 1 ; c_k = 0, k \neq 0$
	$\sum_{k=-\infty}^{\infty} \frac{2 \sin k\omega_o T_1}{k} \delta(\omega - k\omega_o)$	$c_k = \frac{\sin k\omega_o T_1}{k\pi}, k \neq 0 ; c_0 = \frac{2T_1}{T_0}$
$\delta_T(t) = \sum_{k=-\infty}^{\infty} \delta(t - kT)$	$\omega_o \delta_{\omega_o}(\omega) = \frac{2\pi}{T} \sum_{k=-\infty}^{\infty} \delta(\omega - k\frac{2\pi}{T})$	$c_k = \frac{1}{T}$
$p_\tau(t) = \begin{cases} 1, &  t  < \tau \\ 0, &  t  > \tau \end{cases}$	$\frac{2 \sin \omega \tau}{\omega}$	—
$\frac{\sin \omega_o t}{\pi t}$	$p_{\omega_o}(\omega) = \begin{cases} 1, &  \omega  < \omega_o \\ 0, &  \omega  > \omega_o \end{cases}$	—
$\delta(t)$	$1(\text{constanta})$	—
$\delta(t - t_o), t_o \in R$	$e^{-j\omega t_o}$	—
$\sigma(t)$	$\frac{1}{j\omega} + \pi \delta(\omega)$	—
$e^{-at} \sigma(t); \text{Re}\{a\} > 0$	$(a + j\omega)^{-1}$	—
$t e^{-at} \sigma(t); \text{Re}\{a\} > 0$	$(a + j\omega)^{-2}$	—
$\frac{t^{n-1} e^{-at}}{(n-1)!} \sigma(t); \text{Re}\{a\} > 0$	$(a + j\omega)^{-n}$	—